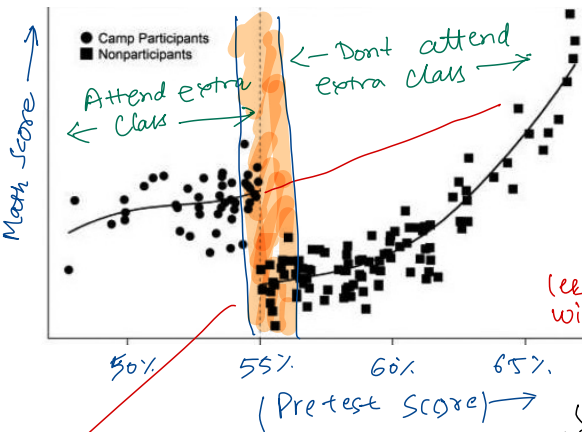
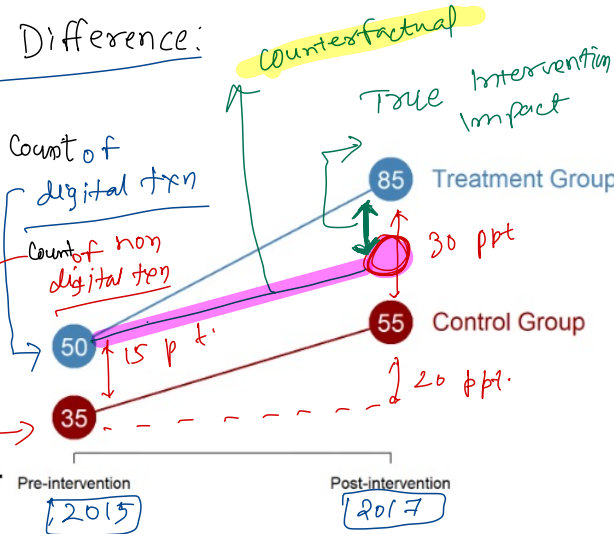
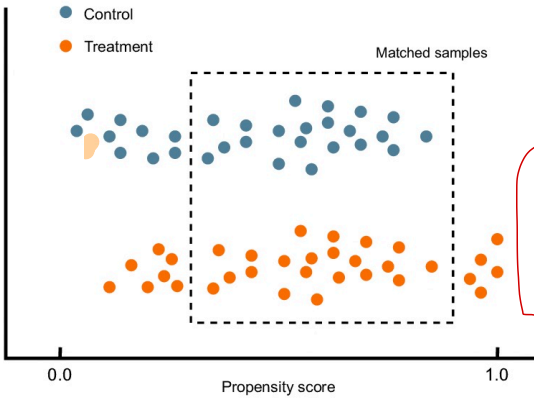


# Estimating Causal Effects

Doing RCT is not always possible. (due to budget, ethical)  
 We employ Retrospective data study to evaluate causal effects.

- Propensity Matching Samples → Algorithm → (Propensity score)
- (Statistical Equivalence of some property)
- Regression Discontinuity:
- Difference-in-Difference:



- ① Extrapolation doesn't work if underlying trend itself is not linear
  - ② PPI who got 54% & PPI who got 56% are same.
- (+2)  
 (less than 55% (agg.) will attend extra class of math)
- Neighborhood acts as proxy for RCT and we can evaluate Avg. Treatment Effect (ATE).



Threat: The admin can lower the scores artificially to increase the exposure.

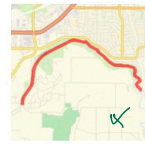
Hide: Assignment Rule from Admin.



10 am 1<sup>st</sup> June ☀️



125 sec



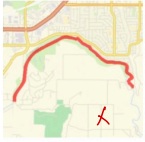
10 am 1<sup>st</sup> June ☀️



118 sec

(20 sec)

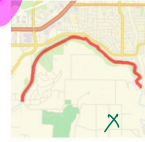
13 sec diff is attributed to weather + shoes



10 am 2<sup>nd</sup> June ☀️



145 sec



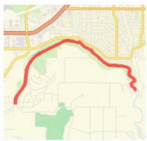
10 am 2<sup>nd</sup> June ☀️



125 sec

$$\left[ \left( \text{☀️} - \checkmark \text{☀️} \right) + \left( \text{👟} - \checkmark \text{👟} \right) \right] = 20 \text{ sec}$$

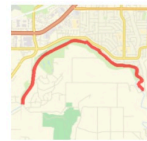
$$\left[ \left( \text{☀️} - \checkmark \text{☀️} \right) + \left( \text{👟} - \checkmark \text{👟} \right) \right] = 7 \text{ sec} = 13 \text{ sec}$$



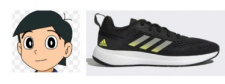
10 am 1<sup>st</sup> June ☀️



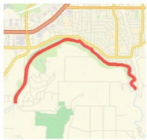
125



10 am 1<sup>st</sup> June ☀️



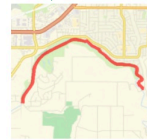
118



10 am 2<sup>nd</sup> June ☀️



145



10 am 2<sup>nd</sup> June ☀️

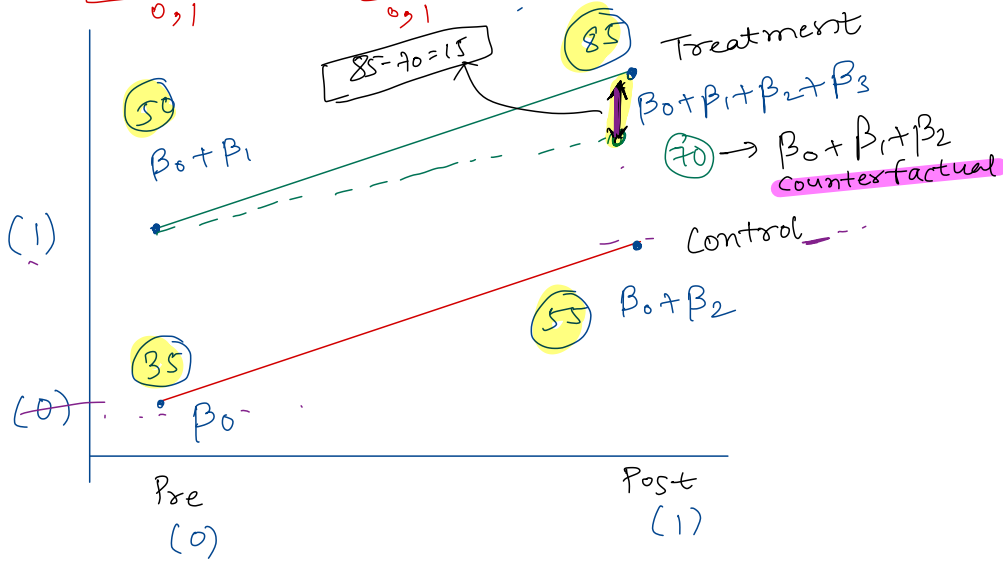


(128 sec)

$$\left( \text{☀️} - \checkmark \text{☀️} \right) \left( \text{👟} - \checkmark \text{👟} \right) = 20 - 10 = 10 \text{ sec}$$

10 sec is attributed solely to the change in shoes.

$$y = \beta_0 + \beta_1 \text{Treatment} + \beta_2 \text{Post} + \beta_3 \text{Treatment} \times \text{Post}$$



$$y = \beta_0 + \beta_1 \text{Treatment} + \beta_2 \text{Post} + \beta_3 \text{Treatment} \times \text{Post}$$

Post = 0, Treatment = 0 ;  $y = \beta_0 \longrightarrow 35$

Post = 0, Treatment = 1 ;  $y = \beta_0 + \beta_1 \longrightarrow 50$

Post = 1, Treatment = 0 ;  $y = \beta_0 + \beta_2 \longrightarrow 55$

Post = 1, Treatment = 1 ;  $y = \beta_0 + \beta_1 + \beta_2 + \beta_3 \longrightarrow 85$

- $\beta_0: 35$
- (T)  $\beta_1: 15$
- (P)  $\beta_2: 20$
- (T x P)  $\beta_3: 15$

Estimating True Impact had there been <sup>no</sup> intervention

$$(\text{Treatment}_{\text{post}} - \text{Treatment}_{\text{pre}}) = (\text{Control}_{\text{post}} - \text{Control}_{\text{pre}})$$

$$(X - 50) = (55 - 35)$$

$$X = 70$$

In mathematical terms, we are interested in estimating 3 coefficients, as in the following equation:

$$Y = \beta_0 + \beta_1 * \text{Treatment} + \beta_2 * \text{Post} + \beta_3 * \text{Treatment} * \text{Post} + e$$

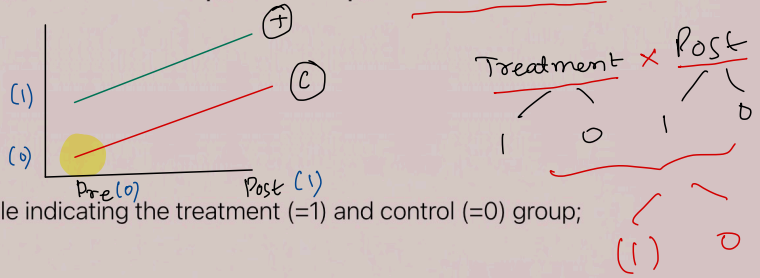
Where:

Y is our outcome variable;

**Treatment** is a dummy variable indicating the treatment (=1) and control (=0) group;

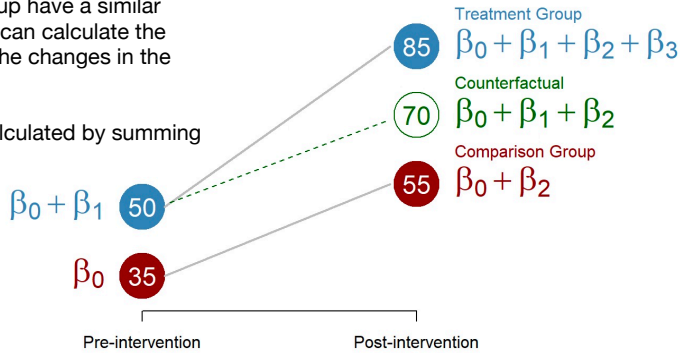
**Post** is a dummy variable indicating pre (=0) and post (=1) treatment;

**Treatment \* Post** is a dummy variable indicating whether the outcome was observed in the treatment AND it was observed after the intervention (=1), or any other case (=0).



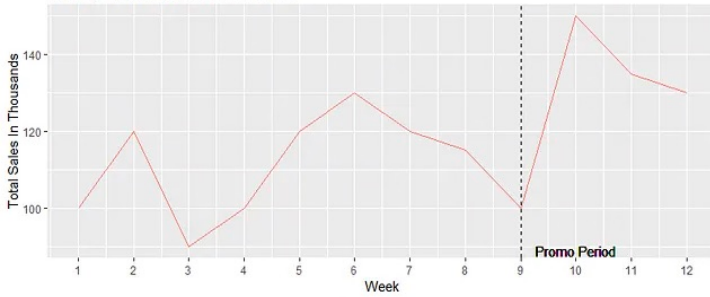
The difference-in-difference model assumes that - in the absence of treatment - the treatment and control group have a similar trend over time, so as we can calculate the counterfactual based on the changes in the control group

Why: Counterfactual is calculated by summing



$\beta$	HYPOTHESES
$b_0$	Is the average outcome of the control group before the treatment $\neq 0$ ?
$b_1$	Is the difference between the control and treatment group before the treatment $\neq 0$ ?
$b_2$	Is the difference between the average outcome of the control group before and after the treatment $\neq 0$ ?
$b_3$	Difference in difference estimator. Does the treatment have an impact?

## Weekly Sales Revenue of Store A



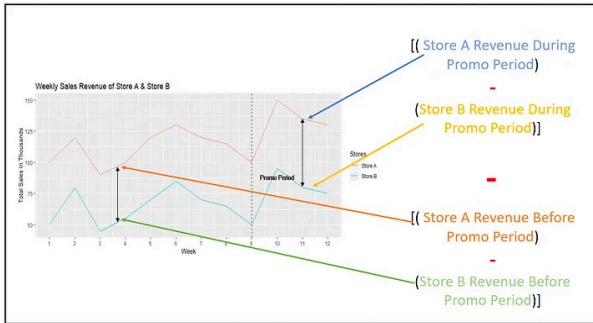
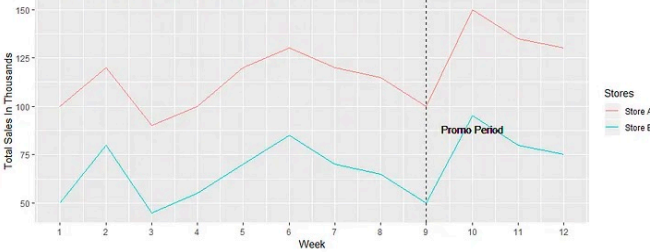
```
Call:
lm(formula = Sales ~ Post_Promotion, data = storeA)

Residuals:
    Min       1Q   Median       3Q      Max
-20.5556 -10.5556  0.5556   9.4444  19.4444

Coefficients:
(Intercept)      110.556      4.267  25.908  1.69e-10 ***
Post_Promotion    27.778      8.535   3.255  0.00865 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 12.8 on 10 degrees of freedom
Multiple R-squared:  0.5144, Adjusted R-squared:  0.4658
F-statistic: 10.59 on 1 and 10 DF, p-value: 0.008651
```

## Weekly Sales Revenue of Store A & Store B



```
Call:
lm(formula = Sales ~ Post_Promotion + Test_Group + Post_Promotion *
  Test_Group, data = StoreAB)

Residuals:
    Min       1Q   Median       3Q      Max
-20.5556 -10.5556 -0.8333  9.4444  21.6667

Coefficients:
(Intercept)      63.333      4.381  14.455  4.75e-12 ***
Post_Promotion  20.000      8.763   2.282  0.0336 *
Test_Group     47.222      6.196   7.621  2.45e-07 ***
Post_Promotion:Test_Group  7.778     12.393   0.628  0.5374
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 13.14 on 20 degrees of freedom
Multiple R-squared:  0.8322, Adjusted R-squared:  0.8071
F-statistic: 33.07 on 3 and 20 DF, p-value: 6.021e-08
```

### Assumptions for Difference in Difference

1. Parallel Trend Assumptions: The counterfactual is considered to have parallel trends with the treatment group. Statistically, counterfactuals can be obtained by performing Dynamic Diff-in-Diff as well
2. Stable Unit Treatment Value Assumption (SUTVA)
  - a). The composition of the treatment and control group is stable for repeated cross-sectional design
  - b). No interference effect: The outcome of treatment should not be impacted by the interaction between the members of the treatment and control group
3. There should not be any Anticipation Effect: The analysis results will be biased if the customers will know about the promotions from before.